'Shine like a lantern in the presence of the Lord.'


# YEAR 5 AND 6 MATHEMATICS CALCULATION METHODS 

```
Always think:
Can I do it mentally?
Can I do it with jottings?
Do I need a written method (vertical layout)?
Do I need a calculator?
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## MENTAL ADDITION GUIDELINES

## Year 5

(MENTAL CALCULATION supported with jottings)

## Using place value (KF)

Count in $0.1 \mathrm{~s}, 0.01 \mathrm{~s}$
e.g. Know what 0.1 more than 0.51 is

| 10 s | Is | 0.1 s | 0.01 s |
| :---: | :---: | :---: | :---: |
|  | 0 | 5 | 1 |

Partitioning (KF)
e.g. $2 \cdot 4+5 \cdot 8=2+5+0.4+0 \cdot 8$

$$
=7+1 \cdot 2
$$

$$
=8 \cdot 2
$$

| 0.1 | 0.2 | $0 \cdot 3$ | 0.4 | 0.5 | 0.6 | 0.7 | 0.8 | 0.9 | 1 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| H | $1 \cdot 2$ | $1 \cdot 3$ | $1 \cdot 4$ | 1.5 | 1.6 | 1.7 | $1 \cdot 8$ | 1.9 | 2 |
| 2.1 | $2 \cdot 2$ | $2 \cdot 3$ | $2 \cdot 4$ | 2.5 | 2.6 | 2.7 | 2.8 | 2.9 | 3 |
| $3 \cdot 1$ | $3 \cdot 2$ | $3 \cdot 3$ | $3 \cdot 4$ | 3.5 | $3 \cdot 6$ | 3.7 | $3 \cdot 8$ | 3 | 4 |
| 41 | $4 \cdot 2$ | 43 | $4 \cdot 4$ | 45 | 4.6 | 4.7 | 48 | 4.9 | 5 |
| 51 | $5 \cdot 2$ | $5 \cdot 3$ | $5 \cdot 4$ | $5 \cdot 5$ | $5 \cdot 6$ | 5.7 | $5 \cdot 8$ | $5 \cdot 9$ | 6 |
| 6.1 | $6 \cdot 2$ | $6 \cdot 3$ | $6 \cdot 4$ | 6.5 | 6.6 | 6.7 | $6 \cdot 8$ | 6. | 7 |
| 74 | $7 \cdot 2$ | $7 \cdot 3$ | 7.4 | 7.5 | 7.6 | 7.7 | 78 | 7.9 | 8 |
| 8.1 | 8.2 | 83 | 8.4 | 8.5 | $8 \cdot 6$ | $8 \cdot 7$ | 88 | 8 | q |
| 9.1 | 9.2 | $9 \cdot 3$ | 9.4 | 9.5 | 9.6 | 9.7 | 98 | 9.9 | 10 |

Children can be supported by visual apparatus / representations of mixed numbers when they are first learning this method

## Year 5

(MENTAL CALCULATION supported with jottings)

## Counting on

Add two decimal numbers by adding the 1 s , then the $0.1 \mathrm{~s} / 0.01 \mathrm{~s}$
e.g. $5 \cdot 72+3.05$ as $5.72+3(8.72)+0.05=8.77$

Add near multiples of 1 (Adjusting Method)
e.g. $6.34+0.99$
e.g. $5 \cdot 63+0.9$

Count on from large numbers
e.g. $6834+3005$ as $9834+5$

## Using number facts (KF)

Number bonds to 1 to 1 decimal place (dp) and to the next whole number (e.g. $5 \cdot 7+$ $0 \cdot 3$
e.g. $0.4+0.6$


Number bonds to 10 to 1 decimal place (dp) / Add to the next 10 from a decimal number.
e.g. $7 \cdot 8+2 \cdot 2=10$
e.g. $3.6+6.4=10$

A number line can be used to support children whilst learning and using these mental methods of addition.

## MENTAL ADDITION GUIDELINES

## Year 6 <br> (MENTAL CALCULATION supported with jottings)

## Using place value

Count in $0.1 \mathrm{~s}, 0.01 \mathrm{~s}, 0.001 \mathrm{~s}$
e.g. Know what 0.001 more than 6.725 is

Partitioning
e.g. $9.54+3.23=9+3+0.5+0.2+0.04+0.03$

$$
=12+0.7+0.07
$$

$$
=12 \cdot 77
$$

## Counting on

Add two decimal numbers by adding the 1 s , then the
$0.1 \mathrm{~s} / 0.01 \mathrm{~s} / 0.001 \mathrm{~s}$
e.g. $6 \cdot 314+3 \cdot 006$ as $6.314+3(9 \cdot 314)+0 \cdot 006=9 \cdot 32$

Add near multiples of 1 (Adjusting Method)
e.g. $6 \cdot 345+0.999$
e.g. $5 \cdot 673+0.9$

Count on from large numbers
e.g. $16375+12003$ as $16375+12000(28375)+3$

## Year 6

 (MENTAL CALCULATION supported with jottings)Using number facts (KF)
Number bonds to 1 up to 3 decimal places (dp) and to the next multiple of 1
e.g. $0.4+0.6$
e.g. $0.63+0.37$
e.g. $0.207+0.793$
e.g. $4.2+0.8$
e.g. $3.67+0.33$
e.g. $2 \cdot 355+0.645$


Number bonds to 10 to 2 decimal places (dp) / Add to the next 10 .
e.g. $4 \cdot 62+5 \cdot 38$
e.g. $7.08+2.92$

| WRITEN ADDITION GUIDELINES |  |
| :---: | :---: |
| Year 5 Written Addition | Year 6 Written Addition |
| Expanded column addition for money leading to compact column addition for adding several amounts of money. <br> e.g. $£ 14 \cdot 64+£ 28 \cdot 78+£ 12 \cdot 26$ $\begin{array}{rrr} £ 14 & 60 p & 4 p \\ £ 28 & 70 p & 8 p \\ +\quad £ 12 & 20 p & 6 p \\ £ 1 & 10 p & \\ \hline £ 55 & 60 p & 8 p \\ \hline \end{array}$ <br> Compact column addition to add pairs of numbers up to 5-digits. e.g. $12350+4921$ $\begin{array}{r} 12350 \\ +\quad 4921 \\ \hline 1 \\ \hline 17271 \\ \hline \end{array}$ <br> Continue to use column addition to add towers of several larger numbers. <br> Use compact addition to add decimal numbers with up to 2 decimal places. <br> e.g. $15 \cdot 68+27 \cdot 86$ $\begin{array}{r} 15.68 \\ +27.86 \\ 11.1 \\ \hline 43.54 \\ \hline \end{array}$ <br> Add related fractions: $\text { e.g. } 3 / 4+1 / 8=7 / 8$ | Compact column addition for adding several large numbers and decimal numbers with up to 2 decimal places. <br> Compact column addition with money e.g. £14•64 + £28•78 + £12•26 $\begin{array}{r} £ \mid 4.64 \\ +£ 28.78 \\ £ \mid 2.26 \\ \frac{11.1}{} \\ \hline £ 55.68 \\ \hline \end{array}$ <br> Add unlike fractions, including mixed numbers $\text { e.g. } 1 / 4+2 / 3=11 / 12$ $\text { e.g. } 2^{1 / 4}+1^{1 / 3}=3^{7 / 12}$ <br> When working out decimal additions children may benefit from reverting back to a number line and their knowledge of place value (KF) to support them: $\begin{aligned} 35.8+7.3 & =35.8+7+0.3 \\ & =42.8+0.3 \\ & =43.1 \end{aligned}$ |

## MENTAL SUBTRACTION GUIDELINES

| Year 5(MENTAL CALCULATION supported with jottings |  |
| :---: | :---: |
| Taking away |  |
| Use place value to subtract decimals |  |
| e.g. $4.58-0.08$ |  |
| e.g. $6.26-0.2$ |  |
| Take away multiples of powers of 10 |  |
| e.g. $15672-300$ |  |
| e.g. $4 \cdot 82-2$ |  |
| e.g. $2.71-0.5$ |  |
| e.g. $4.68-0.02$ |  |
| Partitioning or counting back |  |
| e.g. $3964-1051=3964-1000$ | e.g. $5 \cdot 72-2.01=5.72-2.00$ |
| $=2964-50$ | = $3.72-0.01$ |
| = 2914-1 | $=3.71$ |
| $=2913$ |  |

Subtract near multiples of $1,10,100,1000,10000$ or $£ 1$ (Adjusting Method) e.g. $86456-9999$
e.g. $3.58-1.99$

## Counting up

Find a difference between two numbers by counting up from the smaller to the larger e.g. £12.05-£9. 59
e.g. $2009-869$
$1+30+100+1000+9=1140$

(MENTAL CALCULATION supported with jottings)
Find change using shopkeepers' addition
e.g. Buy a toy for $£ 6.89$ using $£ 10.00$

$$
1 p+10 p+£ 3.00
$$



Find a difference between two amounts of money by counting up

## Using number facts (KF)

Derived facts from number bonds to 10 and 100
e.g. $2-0.45$ using $45+55=100$
e.g. $3-0.86$ using $86+14=100$


Number bonds to $£ 1, £ 10$ and $£ 100$ (KF)
e.g. £4.00-£3.86
e.g. $£ 100-£ 66$ using $66+34=100$

## MENTAL SUBTRACTION GUIDELINES

| Year 6 <br> (MENTAL CALCULATION supported with jottings) | Year 6 <br> (MENTAL CALCULATION supported with jottings) |
| :---: | :---: |
| Taking away <br> Use place value to subtract decimals <br> e.g. $7.782-0.08$ <br> e.g. $16.263-0.2$ <br> Take away multiples of powers of 10 <br> e.g. $132956-400$ <br> e.g. $686109-40000$ <br> e.g. $7.823-0.5$ <br> Partitioning or counting back <br> e.g. $3964-1051=3964-1000$ $=2964-50$ $=2914-1$ $\text { e.g. } \begin{aligned} 5 \cdot 72-2 \cdot 01 & =5.72-2.00 \\ & =3.72-0.01 \\ & =3.71 \end{aligned}$ $=2913$ <br> Subtract near multiples of $1,10,100,1000,10000$ or $£ 1$ <br> e.g. $360078-99998$ <br> e.g. $12.831-0.99$ | Counting up <br> Find a difference between two decimal numbers by counting up from the smaller to the larger <br> e.g. 1.2-0.87 <br> Using number facts <br> Derived facts from number bonds to 10 and 100 (KF) <br> e.g. $0 \cdot 1-0.075$ using $75+25=100$ <br> e.g. $5-0.65$ using $65+35=100$ <br> Number bonds to $£ 1, £ 10$ and $£ 100$ (KF) <br> e.g. £7.00-£4.37 <br> e.g. $£ 100-£ 66 \cdot 20$ using $20 p+80 p=£ 1$ and $£ 67+£ 33=£ 100$ |


| WRITTEN SUBTRACTION GUIDELIES |  |
| :---: | :---: |
| Year 5 Written Subtraction | Year 6 Written Subtraction |
| Compact column subtraction for numbers with up to 5 digits e.g. $16324-8516$ $\begin{array}{rrrrr} 0 & 15 & 13 & 1 & 14 \\ x & 6 & \not x & 2 & \not k \\ - & 8 & 5 & 1 & 6 \\ \hline 7 & 8 & 0 & 8 \\ \hline \end{array}$ | Compact column subtraction for large numbers e.g. $34685-16458$ $\begin{array}{rrrrr} 2 & 14 & 7 & 15 \\ \not 8 & 4 & 6 & 8 & 8 \\ -1 & 6 & 4 & 5 & 8 \\ \hline 1 & 8 & 2 & 2 & 7 \\ \hline \end{array}$ |
| Continue to use counting up subtraction for subtractions involving money, including finding change e.g. £50-£28•76 | Use counting up for subtractions where the larger number is a multiple or near multiple of 1000 or 10000 <br> Use counting up subtraction when dealing with money e.g. $£ 100-£ 78.56$ e.g. $£ 45 \cdot 23-£ 27.57$ |
| Use counting up subtraction to subtract decimal numbers $\begin{aligned} & \text { e.g. } 4 \cdot 2-1 \cdot 74 \\ & \quad 0.06+0.2+2+0.2=2.46 \\ & +0.06+0.2 \end{aligned}$ | Use counting up subtraction to subtract decimal numbers $\begin{aligned} & \text { e.g. } 13 \cdot 1-2.37 \\ & \quad 0.03+0.6+10+0.1=10.73 \end{aligned}$ $10$ |
|  |  |
| Subtract related fractions <br> e.g. $3 / 4-1 / 8=5 / 8$ <br> NB Counting up subtraction provides a default method for ALL children | Subtract unlike fractions, including mixed numbers <br> e.g. $3 / 4-1 / 3=5 / 12$ <br> e.g. $2^{3} / 4-1 \frac{1}{3} / 3=15 / 12$ <br> NB Counting up subtraction provides a default method for ALL children |

## MENTAL MULTIPLICATION GUIDELINES

## Year 5

(MENTAL CALCULATION supported with jottings and practical apparatus)

## Doubling and halving

Double amounts of money using partitioning
e.g. double $£ 6.73$


Use doubling and halving as a strategy in multiplying by 2, 4, 8, 5 and $20(\mathbf{K F})$ e.g. $58 \times 5$ is half of $58 \times 10(580)=290$

## Grouping

Multiply whole numbers and decimals by 10, 100, 1000
e.g. $3.4 \times 100=340$

Use partitioning to multiply 'friendly' 2 and 3 -digit numbers by 1 -digit numbers e.g. $402 \times 6$ as $400 \times 6(2400)$ and $2 \times 6(12)=2412$


Use partitioning to multiply decimal numbers by 1 -digit numbers e.g. $4.5 \times 3$ as $4 \times 3(12)$ and $0.5 \times 3(1.5)=13.5$

Multiply near multiples by rounding
e.g. $32 \times 29$ as $(32 \times 30)-32=928$
(MENTAL CALCULATION supported with jottings and practical apparatus)

## Using number facts

Use times-tables facts up to $12 \times 12$ to multiply multiples of $10 / 100$ of the multiplier. (KF)
e.g. $4 \times 6=24$

Therefore $40 \times 6=240$
and
$400 \times 6=2400$

Use knowledge of factors (KF) and multiples (KF) in multiplication
e.g. $43 \times 6$ is double $43 \times 3$
e.g. $28 \times 50$ is half of $28 \times 100(2800)=1400$

Know square numbers and cube numbers (KF)


## MENTAL MULTIPLICATION GUIDELINES

## Year 6

(MENTAL CALCULATION supported with jottings and practical apparatus)

## Doubling and halving

Double decimal numbers with up to 2 places using partitioning e.g. double 36.73


Use doubling and halving as strategies in mental multiplication

## Grouping

Use partitioning as a strategy in mental multiplication, as appropriate
e.g. $3060 \times 4$ as $3000 \times 4(12000)$ and $60 \times 4(240)=12240$
e.g. $8.4 \times 8$ as $8 \times 8(64)$ and $0.4 \times 8(3 \cdot 2)=67.2$

Use factors in mental multiplication
e.g. $421 \times 6$ as $421 \times 3$ (1263) doubled $=2526$
e.g. $3.42 \times 5$ as half of $3.42 \times 10=17.1$

Multiply decimal numbers using near multiples by rounding
$\times 6 \times 6$ e.g. $4.3 \times 19$ as $(4.3 \times 20)-4.3=81 \cdot 7$
(MENTAL CALCULATION supported with jottings and practical apparatus)

## Using number facts (KF)

Use times-tables facts up to $12 \times 12$ in mental multiplication of large numbers or numbers with up to 2 decimal places
e.g. $6 \times 4=24$ and $0.06 \times 4=0.24$


## MENTAL DIVISION GUIDELINES

## Year 5

(MENTAL CALCULATION supported with jottings and practical apparatus)

## Doubling and halving

Halve amounts of money using partitioning.
e.g. half of $£ 14.84$ is half of $£ 14$ ( $£ 7$ ) plus half of 84 p (42p)


Use doubling and halving as a strategy in dividing by 2, 4, 8, 5 and 20
e.g. $115 \div 5$ as double $115(230) \div 10=23$

## Grouping

Divide numbers by 10, 100, 1000 to obtain decimal answers with up to 3 decimal places. (KF)
e.g. $340 \div 100=3.4$

Use the $10^{\text {th }}, 20^{\text {th }}, 30^{\text {th }} \ldots$ multiple of the divisor to divide 'friendly' 2 and 3 -digit numbers by 1 -digit numbers.
e.g. $186 \div 6$ as $30 \times 6$ (180) and $1 \times 6$ (6)

(MENTAL CALCULATION supported with jottings and practical apparatus)

## Using number facts

Use division facts from the times-tables up to $12 \times 12$ to divide multiples of powers of 10 of the divisor (KF)
e.g. $3600 \div 9$ using $36 \div 9$

Know square numbers and cube numbers (KF)


## MENTAL DIVISION GUIDELINES

## Year 6

(MENTAL CALCULATION supported with jottings and practical apparatus)

## Doubling and halving

Halve decimal numbers with up to 2 places using partitioning.
e.g. half of 36.86 is half of $36(18)$ plus half of $0.86(0.43)$


Use doubling and halving as strategies in mental division.

## Grouping

Use the 10th, 20th, 30th ... or 100th, 200th, 300th ... multiples of the divisor to divide large numbers.
e.g. $378 \div 9$ as $40 \times 9(360)$ and $2 \times 9(18)$
$378 \div 9=\square$

$$
\times 9=378 \quad 378 \div 9=42
$$

$40 \times 9=360$
18
$2 \times 9=18$

42

Use tests for divisibility (KF)
e.g. 135 divides by 3 , as $1+3+5=9$ and 9 is in the $\times 3$ table
(MENTAL CALCULATION supported with jottings and practical apparatus)

## Using number facts

Use division facts from the times-tables up to $12 \times 12$ to divide decimal numbers by 1 digit numbers
e.g. $1 \cdot 17 \div 3$ is $1 / 100$ of $117 \div 3$ (39)

Know tests of divisibility for numbers divisible by $2,3,4,5,9,10$ and 25 (KF)

## WRITTEN DIVISION GUIDELINES



Short division of 3- and 4-digit numbers by 1-digit numbers.
e.g. $139 \div 3$

$$
\begin{aligned}
& 46 \mathrm{rl} \\
& 3 \longdiv { 1 3 ^ { 1 9 } }
\end{aligned}
$$

Use chunking

| $326 \div 6$ |  |
| :--- | :--- |
|  |  |
| -326 |  |
| $-\quad 300$ |  |
| 26 | $(50 \times 6)$ |
| $-\quad 24$ | Answer: |
| -0 | $5 \times 6)+4=54$ |

$$
\begin{aligned}
& \text { Key Facts } \\
& 6 \times 1=6 \\
& 6 \times 2=12 \\
& 6 \times 5=30 \\
& 6 \times 10=60
\end{aligned}
$$

## Year 6

Written Division
Give remainders as whole numbers or as fractions.
Find unit and non-unit fractions of large amounts.
e.g. $3 / 5$ of 265 is $3 \times(265 \div 5)=159$

Turn improper fractions into mixed numbers and vice versa
Short division of 3- and 4-digit numbers by 1-digit numbers e.g. $139 \div 3$


Long division of 3 - and 4-digit numbers by 2-digit numbers. e.g. $4176 \div 13$

$$
\begin{aligned}
& 300+20+1, r 3 \\
& \begin{array}{l}
4176 \\
-3900 \\
276 \\
-260 \\
16
\end{array} \\
& \frac{-13}{3}
\end{aligned}
$$

Give remainders as whole numbers, fractions or decimals.
Use place value to divide 1 - and 2-place decimals by numbers $\leq 12$.
e.g. $3.65 \div 5$ as $(365 \div 5) \div 100=0.73$

Divide proper fractions by whole numbers

